## Assignment 11 (Sol.) Reinforcement Learning Prof. B. Ravindran

## 1. Using the MAXQ approach leads to solutions which are

- (a) hierarchically optimal
- (b) recursively optimal
- (c) flat optimal

## **Sol.** (b)

Since the MAXQ policy of the core MDP is the set of policies of individual sub-tasks, with individual sub-task policies aiming to solve the sub-tasks optimally, you can expect to obtain recursively optimal solutions using the MAXQ approach.

- 2. We saw that each sub-task has an associated pseudo-reward function. Are the rewards of the core MDP available to the agent while it is learning policies of individual sub-tasks or is the agent restricted to the corresponding sub-task's pseudo rewards?
  - (a) only pseudo rewards are available
  - (b) both pseudo rewards and core MDP rewards are available

## **Sol.** (b)

As we observed in the example taxi problem, rewards of the core MDP are available while learning the policies of the sub-tasks.

- 3. In the MAXQ framework, is termination in a sub-task deterministic or stochastic as in the options framework?
  - (a) deterministic
  - (b) stochastic

**Sol.** (a)

We saw in the sub-task definition that for each sub-task, all states of the core MDP are partitioned into a set of active states and a set of terminal states, where sub-task termination is immediate (and deterministic) whenever a terminal state is entered.

- 4. Each sub-task  $M_i$  is an SMDP because
  - (a) the state space of the sub-task is a subset of the state space of the core MDP
  - (b) each sub-task has its own policy

- (c) actions in a sub-task can be temporally extended
- (d) the rewards received in sub-tasks depend not only on the state but also on the sub-task in which an action was executed

In the definition, we saw that the actions in a sub-task comprise both, primitive actions as well as other sub-tasks. The invocation of a sub-task results in a sequence of actions being executed (similar to an option). Thus, each sub-task is an SMDP.

5. The expected reward function  $\bar{R}(s, a)$  of the SMDP corresponding to sub-task  $M_i$  is equivalent to the projected value function  $V^{\pi_i}(a, s)$ . True or false?

(a) false

(b) true

**Sol.** (a) Recall that  $\bar{R}(s, a) = V^{\pi}(a, s)$  not  $V^{\pi_i}(a, s)$ .

6. In the MAXQ approach to solving a problem, suppose that sub-task  $M_i$  invokes sub-task  $M_j$ . Do the pseudo rewards of  $M_j$  have any effect on sub-task  $M_i$ ?

(a) no

(b) yes

**Sol.** (b)

The pseudo rewards of one sub-task are not directly considered when solving a different subtask regardless of their connectivity. However, since sub-task  $M_i$  invokes sub-task  $M_j$ , and hence depends upon the policy of  $M_j$ , the rewards of  $M_j$  do effect sub-task  $M_i$ , as the pseudo rewards of sub-task  $M_j$  would be a factor determining the policy of  $M_j$ .

**Sol.** (c)